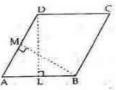
### Question 2:

Since ABCD is a parallelogram and DL is perpendicular to AB.



So, its area = AB 
$$\times$$
 DL =  $(10 \times 6)$  cm<sup>2</sup>

 $=60 \, \text{cm}^2$ 

Also, in parallelogram ABCD, BM LAD

... Area of parallelogram ABCD = AD × BM

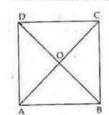
$$AD \times 8 = 60$$

$$AD = \frac{60}{8} = 7.5 \text{ cm}$$

# Question 3:

ABCD is a rhombus in which diagonal AC=24 cm and BD=16 cm

These diagonals intersect at O.



Since diagonals of a rhombus are perpendicular to each other. So, in  $\Delta$  ACD,

OD is its altitude and AC is itsbase.

So, area of 
$$\triangle ACD = \frac{1}{2} \times AC \times OD$$

$$= \frac{1}{2} \times 24 \times \frac{BD}{2}$$

$$= \left(\frac{1}{2} \times 24 \times 8\right) \text{ cm}^2 \quad \text{[:BD = 16 cm]}$$

=300

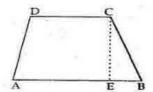
Area of 
$$\triangle$$
 ABC =  $\frac{1}{2} \times$  AC  $\times$  OB  
=  $\left(\frac{1}{2} \times 24 \times 8\right)$  cm<sup>2</sup> = 96 cm<sup>2</sup>

Now, area of rhombus = Area of  $\triangle$  ACD + Area of  $\triangle$  ABC = (96 + 96) cm<sup>2</sup>

$$= 192 \text{ cm}^2$$

### Question 4:

ABCD is a trapezium in which, AB ||CD AB=9 cm and CD= 6 cm CE is a perpendicular drawn to AB through C and CE= 8 cm



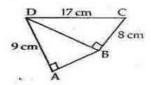
Area of trapezium= $\frac{1}{2}$ (sum of parallel sides)×distancebetween them

$$= \left[ \frac{1}{2} (9+6) \times 8 \right] \text{ cm}^2$$
$$= \left[ \frac{1}{2} \times 15 \times 8 \right] \text{ cm}^2 = 60 \text{ cm}^2$$

: Area of trapezium = 60 cm²

### Question 5:

(I) ABCD is a quadrilateral.



Now in right angled A DBC,

$$DB^2 = DC^2 - CB^2$$

$$=17^2-8^2$$

So, area of 
$$\triangle DBC = \left(\frac{1}{2} \times 15 \times 8\right) \text{ cm}^2 = 60 \text{ cm}^2$$

Again, in right angled ΔDAB,

$$AB^2 = DB^2 - AD^2$$

$$=15^2-9^2$$

$$AB = \sqrt{144} = 12 \text{ cm}$$

area of 
$$\Delta DAB = \left(\frac{1}{2} \times 12 \times 9\right) \text{cm}^2 = 54 \text{ cm}^2$$

So, area of quadrillateral ABCD

$$= (60 + 54) \text{ cm}^2 = 114 \text{ cm}^2$$

area of quadrilateral ABCD = 114 cm²



RT 
$$\perp$$
PQ  
In right angled  $\triangle$ RTQ  
RT<sup>2</sup> = RQ<sup>2</sup> - TQ<sup>2</sup>  
= 17<sup>2</sup> - 8<sup>2</sup>  
= 289 - 64 = 225 cm<sup>2</sup>  
RT =  $\sqrt{225}$  = 15 cm

.. Area of trapezium =  $\frac{1}{2}$  (sum of parallel sides) x distance

between them

$$= \frac{1}{2} \times (PQ + SR) \times RT$$

$$= \frac{1}{2} \times (16 + 8) \times 15$$

$$= \left(\frac{1}{2} \times 24 \times 15\right) \text{ cm}^2 = 180 \text{ cm}^2$$
area of trapezium =  $180 \text{ cm}^2$ 

## Question 7:

Given: ABCD is a quadrilateral and BD is one of

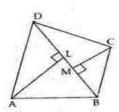
its diagonals.

ALIBD and CMIBD

To Prove: area (quad. ABCD)

 $=\frac{1}{2}\times BD\times (AL+CM)$ 

Proof:



Area of  $\triangle$  BAD =  $\frac{1}{2} \times BD \times AL$ 

Area of  $\triangle$  CBD =  $\frac{1}{2} \times$  BD  $\times$  CM

Area of quard,  $\overrightarrow{ABCD}$  = Area of  $\triangle ABD$  + Area of  $\triangle CBD$ =  $\frac{1}{2} \times BD \times AL + \frac{1}{2} \times BD \times CM$ 

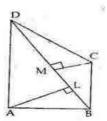
. Area of quard ABCD =  $\frac{1}{2} \times BD[AL + CM]$ 

### Question 8:

Area of 
$$\triangle BAD = \frac{1}{2} \times BD \times AL$$

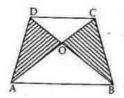
$$= \left(\frac{1}{2} \times 14 \times 8\right) \text{ cm}^2 = 56 \text{ cm}^2$$
Area of  $\triangle CBD = \frac{1}{2} \times BD \times CM$ 

$$= \left(\frac{1}{2} \times 14 \times 6\right) \text{ cm}^2 = 42 \text{ cm}^2$$



: area of quad. ABCD = Area of  $\triangle$  ABD + Area of  $\triangle$  CBD = (56 + 42) cm<sup>2</sup> = 98 cm<sup>2</sup>

## Question 9:



Consider  $\Delta$  ADC and  $\Delta$  DCB. We find they have the same base CD and lie between two parallel lines DC and AB.

Triangles on the same base and between the same parallels are equal in area.

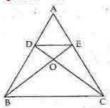
So  $\Delta \text{CDA}$  and  $\Delta \text{CDB}$  are equal in area.

∴ area(ΔCDA)= area(ΔCDB)

Now,  $\operatorname{area}(\Delta \operatorname{AOD}) = \operatorname{area}(\Delta \operatorname{ADC}) - \operatorname{area}(\Delta \operatorname{OCD})$ and  $\operatorname{area}(\Delta \operatorname{BOC}) = \operatorname{area}(\Delta \operatorname{CDB}) - \operatorname{area}(\Delta \operatorname{OCD})$  $= \operatorname{area}(\Delta \operatorname{ADC}) - \operatorname{area}(\Delta \operatorname{OCD})$ 

⇒ area(ΔAOD)= area(ΔBOC)

### Question 10:



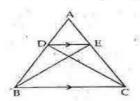
(i) ADBE and ADCE have the same base DE and lie between parallel lines BC and DE.

So, area ( $\Delta$ DBE) = area ( $\Delta$ DCE).....(1) Adding area ( $\Delta$  ADE) on both sides, we get  $ar(\Delta$ DBE) +  $ar(\Delta$ ADE) =  $ar(\Delta$ DCE)+ $ar(\Delta$ ADE)

 $\Rightarrow \qquad \operatorname{ar}(\Delta \mathsf{ABE}) = \operatorname{ar}(\Delta \mathsf{ACD})$ (ii) Since  $\operatorname{ar}(\Delta \mathsf{DBE}) = \operatorname{ar}(\Delta \mathsf{DCE}) \text{ [from (1)]}$ Subtracting  $\operatorname{ar}(\Delta \mathsf{ODE}) \text{ from both sides we get}$   $\operatorname{ar}(\Delta \mathsf{DBE}) - \operatorname{ar}(\Delta \mathsf{ODE}) = \operatorname{ar}(\Delta \mathsf{DCE}) - \operatorname{ar}(\Delta \mathsf{ODE})$   $\Rightarrow \qquad \operatorname{ar}(\Delta \mathsf{OBD}) = \operatorname{ar}(\Delta \mathsf{OCE})$ 

### Question 11:

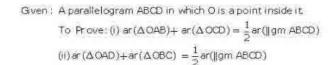
Given: A  $\triangle$ ABC in which points D and E lie on AB and AC, such that ar( $\triangle$ BCE) = ar( $\triangle$ BCD)

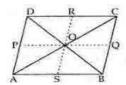


To Prove: DE || BC

Proof : As  $\triangle$ BCE and  $\triangle$  BCD have same base BC, and are equal in area, they have same altitudes. This means that they lie between two parallel lines.  $\therefore$  DE  $\parallel$  BC

### Question 12:





Construction: Through O draw PQ ||AB and RS|| AD Proof: (i)  $\Delta$  AOB and parallelogram ABQP have same base AB and lie between parallel lines AB and PQ. If a triangle and a parallelogram are on the same base, and between the same parallels, then the area of the triangle is equal to half the area of the parallelogram.

$$ar(\Delta AOB) = \frac{1}{2}ar(\|gm ABQP)$$
Similarly, 
$$ar(\Delta COD) = \frac{1}{2}ar(\|gm PQCD)$$
So, 
$$ar(\Delta AOB) + ar(\Delta COD)$$

$$= \frac{1}{2}ar(\|gm ABQP) + \frac{1}{2}ar(\|gm PQCD)$$

$$= \frac{1}{2}[ar(\|gm ABQP) + ar(\|gm PQCD)]$$

$$= \frac{1}{2}[ar\|gm ABQD]$$

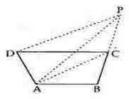
 Δ AOD and | gm ASRD have the same base AD and lie between same parallel lines AD and RS.

So, 
$$\operatorname{ar}(\Delta \mathsf{AOD}) = \frac{1}{2}\operatorname{ar}(\|\mathsf{gm}\ \mathsf{ASRD})$$
  
Similarly,  $\operatorname{ar}(\Delta \mathsf{BOC}) = \frac{1}{2}\operatorname{ar}(\|\mathsf{gm}\ \mathsf{RSBC})$   
 $\therefore \operatorname{ar}(\Delta \mathsf{AOD}) + \operatorname{ar}(\Delta \mathsf{BOC}) = \frac{1}{2}\left[\operatorname{ar}(\|\mathsf{gmASRD}) + \operatorname{ar}(\|\mathsf{gmRSBC})\right]$   
 $= \frac{1}{2}[\operatorname{ar}(\|\mathsf{gmABCD})]$ 

#### Question 13:

Given: ABCD is a quadrilateral in which through D, a line is drawn parallel to AC which meets BC produced in P.

To Prove :  $ar(\triangle ABP) = ar(quad.ABCD)$ 



Priorf:  $\Delta$  ACP and  $\Delta$  ACD have same base AC and lie between parallel lines AC and DP.

$$ar(\Delta ACP) = ar(\Delta ACD)$$

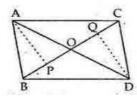
Adding ar ( $\Delta$ ABC) on both sides, we get;

 $ar(\Delta ACP) + ar(\Delta ABC) = ar(\Delta ACD) + ar(\Delta ABC)$ 

ar(ΔABP) = ar (quad ABCD)

## Question 14:

Given: Two triangles, i.e.  $\triangle$  ABC and  $\triangle$  DBC which have same base BC and points A and D lie on opposite sides of BC and ar( $\triangle$ ABC) = ar( $\triangle$ BDC)



To Prove: OA = OD

Construction: Draw AP LBC and DQ LBC

Proof: We have

$$ar(\Delta ABC) = \frac{1}{2} \times BC \times AP \text{ and}$$

$$ar(\Delta BCD) = \frac{1}{2} \times BC \times DQ$$

So, 
$$\frac{1}{2} \times BC \times AP = \frac{1}{2} \times BC \times DQ$$
 [from (1)]

Now, in  $\triangle AOP$  and  $\triangle QOD$ , we have

 $\angle APO = \angle DQO = 90^{\circ}$ 

and  $\angle AOP = \angle DOQ$ 

vertically opp, angles

AP = DQ [from (2)]

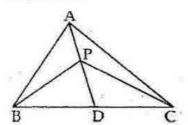
Thus, by Angle-Angle-Side criterion of congruence, we have

 $\triangle AOP \cong \triangle QOD$  [AAS]

The corresponding parts of the congruent triangles are equal.

### Question 15:

Given: A  $\triangle$  ABC in which AD is the median and P is a point on AD.



To Prove: (i)  $ar(\Delta BDP) = ar(\Delta CDP)$ 

(ii)  $ar(\Delta ABP) = ar(\Delta APC)$ 

Proof :(i) In  $\Delta$  BPC, PD is the median Since median of a triangle divides the triangle into two triangles of equal areas

So,  $ar(\Delta BPD) = ar(\Delta CDP).....(1)$ 

(ii) In △ABC, AD is the median

So,  $ar(\triangle ABD) = ar(\triangle ADC)$ 

But,  $ar(\Delta BPD) = ar(\Delta CDP)$  [from (1)]

Subtracting  $ar(\Delta BPD)$  from both the sides

of the equation, we have

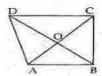
 $\therefore ar(\Delta ABD) - ar(\Delta BPD) = ar(\Delta ADC) - ar(\Delta BPD)$ 

 $=ar(\Delta ADC)-ar(\Delta CDP)$  from (1)

 $\Rightarrow$  ar( $\triangle$ ABP) = ar( $\triangle$ ACP).

# Question 16:

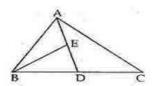
Given: A quadrilateral ABCD in which diagonals AC and BD intersect at O and BO = OD



To Prove :  $\operatorname{ar}(\Delta ABC) = \operatorname{ar}(\Delta ADC)$ Proof: Since OB = OD [Given] So, AO is the median of  $\Delta ABD$ :  $\operatorname{ar}(\Delta AOD) = \operatorname{ar}(\Delta AOB)$  ...(i) As OC is the median of  $\Delta CBD$   $\operatorname{ar}(\Delta DOC) = \operatorname{ar}(\Delta BOC)$  .... (ii) Adding both sides of (i) and (ii), we get  $\operatorname{ar}(\Delta AOD) + \operatorname{ar}(\Delta DOC) = \operatorname{ar}(\Delta AOB) + \operatorname{ar}(\Delta BOC)$ ...  $\operatorname{ar}(\Delta ADC) = \operatorname{ar}(\Delta ABC)$ 

### Question 17:

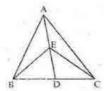
Given : A  $\Delta$  ABC in which AD is a median and E is the mid – point of AD



To Prove:  $\operatorname{ar}(\Delta BED) = \frac{1}{4}\operatorname{ar}(\Delta ABC)$ Proof: Since,  $\operatorname{ar}(\Delta ABD) = \operatorname{ar}(\Delta ACD)$  [: AD is the median] i.e.  $\operatorname{ar}(\Delta ABD) = \frac{1}{2}\operatorname{ar}(\Delta ABC)$  .....(1) [:  $\operatorname{ar}(\Delta ABC) = \operatorname{ar}(\Delta ABD) + \operatorname{ar}(\Delta ADC)$ ] Now, as BE is the median of  $\Delta ABD$   $\operatorname{ar}(\Delta ABE) = \operatorname{ar}(\Delta BED)$  .....(2) Since  $\operatorname{ar}(\Delta ABD) = \operatorname{ar}(\Delta ABE) + \operatorname{ar}(\Delta BED)$  .....(3) .:  $\operatorname{ar}(\Delta BED) = \operatorname{ar}(\Delta ABE)$  [from (2)]  $= \frac{1}{2}\operatorname{ar}(\Delta ABD)$  [from (2) and (3)]  $= \frac{1}{2}[\frac{1}{2}\operatorname{ar}(\Delta ABC)$  [from (1)]  $= \frac{1}{4}\operatorname{ar}(\Delta ABC)$ 

### Question 18:

Given: A  $\triangle$  ABC in which E is the mid – point of line segment AD where D is a point on BC.



To Prove: 
$$\operatorname{ar}(\Delta \operatorname{BEC}) = \frac{1}{2}\operatorname{ar}(\Delta \operatorname{ABC})$$
Proof: Since BE is the median of  $\Delta \operatorname{ABD}$ 
So,  $\operatorname{ar}(\Delta \operatorname{BDE}) = \operatorname{ar}(\Delta \operatorname{ABE})$ 

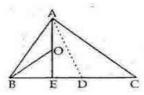
$$\therefore \operatorname{ar}(\Delta \operatorname{BDE}) = \frac{1}{2}\operatorname{ar}(\Delta \operatorname{ABD}) \dots (i)$$
As, CE is median of  $\Delta \operatorname{ADC}$ 
So,  $\operatorname{ar}(\Delta \operatorname{CDE}) = \frac{1}{2}\operatorname{ar}(\Delta \operatorname{ACD}) \dots (ii)$ 
Adding (i) and (ii), we get
$$\operatorname{ar}(\Delta \operatorname{BDE}) + \operatorname{ar}(\Delta \operatorname{CDE}) = \frac{1}{2}\operatorname{ar}(\Delta \operatorname{ABD}) + \frac{1}{2}\operatorname{ar}(\Delta \operatorname{ACD})$$

$$\operatorname{ar}(\Delta \operatorname{BEC}) = \frac{1}{2}\left[\operatorname{ar}(\Delta \operatorname{ABD}) + \operatorname{ar}(\Delta \operatorname{ACD})\right]$$

$$= \frac{1}{2}\operatorname{ar}(\Delta \operatorname{ABC}).$$

### Question 19:

Given: A  $\triangle$  ABC in which AD is the median and E is the mid-point of BD. O is the mid-point of AE.



To Prove :  $ar(\Delta BOE) = \frac{1}{8}ar(\Delta ABC)$ 

Proof: Since O is the midpoint of AE. So, BO is the median of  $\Delta$ BAE

$$\therefore \qquad \text{ar} (\Delta BOE) = \frac{1}{2} \text{ar} (\Delta ABE) \dots (1)$$

Now, E is the mid-point of BD

So AE divides  $\triangle$  ABD into two triangles of equal area.

$$\operatorname{ar}(\Delta ABE) = \frac{1}{2}\operatorname{ar}(\Delta ABD)....(2)$$

As D is the mid point of BC

So 
$$\operatorname{ar}(\Delta ABD) = \frac{1}{2}\operatorname{ar}(\Delta ABC)....(3)$$

$$\Rightarrow \operatorname{ar}(\Delta BOE) = \frac{1}{2}\operatorname{ar}(\Delta ABE) \quad [from (1)]$$

$$= \frac{1}{2}\left[\frac{1}{2}\operatorname{ar}(\Delta ABD)\right] \quad [from (2)]$$

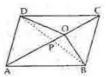
$$= \frac{1}{4}\operatorname{ar}(\Delta ABD)$$

$$= \frac{1}{4} \cdot \frac{1}{2}\operatorname{ar}(\Delta ABC) \quad [from (3)]$$

$$= \frac{1}{8}\operatorname{ar}(\Delta ABC)$$

### Question 20:

Given: A parallelogram ABCD in which O is any point on the diagonal AC.



To Prove:  $ar(\triangle AOB) = ar(\triangle AOD)$ .

Construction: Join BD which intersects AC at P.

Proof: As diagonals of a parallelogram bisect each other,

so, OP is the median of  $\Delta$ ODB

 $ar(\Delta ODP) = ar(\Delta OBP)$ 

Also, APIs the median of AABD

 $ar(\Delta ADP) = ar(\Delta ABP)$ 

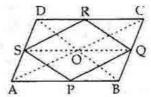
Adding both sides, we get

 $ar(\Delta ODP) + ar(\Delta ADP) = ar(\Delta OBP) + ar(\Delta ABP)$ 

 $\Rightarrow$  ar( $\triangle$ AOD)= ar( $\triangle$ AOB).

### Question 21;

Given: ABCD is a parallelogram and P,Q,R and S are the midpoints of AB,BC,CD and DA respectively.



To Prove: PQRS is a parallelogram and ar (||gmPQRS)

$$=\frac{1}{2} \operatorname{ar} (\|\operatorname{gm} \operatorname{ABCD})$$

Construction: Join AC, BD and SQ.

Proof: As S and R are the midpoints of AD and CD.So, in AADC,

SR | AC | By mid point theorem

Also, as P and Q are the midpoints of AB and BC So, in  $\Delta ABC$ 

PQ | AC

PQ || AC || SR

PQ | SR

Similarly, we can prove SP || RQ.

Thus PQRS is a parallelogram as its opposite sides are parallel since diagonals of a parallelogram bisect each other.

So in AABD,

O is the midpoint of AC and S is the midpoint of AD.

OS | AB By midpoint theorem

Similarly in  $\Delta ABC$ , we can prove that,

OQ AB

i.e.

5Q | AB

Thus, ABQS is a parallelogram.

Now, 
$$ar(\Delta SPQ) = \frac{1}{2}ar(\|gmABQS)$$
 ....(i)

: \(\Delta\text{SPQ}\) and \(\|\text{gm}\) ABQS have the same base and lie between same parallel lines

Similarly, we can prove that;

$$ar(\Delta SRQ) = \frac{1}{2}ar(\|gmSQCD)$$
 ....(ii

Adding (i) and (ii) we get

$$\operatorname{ar}(\Delta \mathsf{SPQ}) + \operatorname{ar}(\Delta \mathsf{SRQ}) = \frac{1}{2} [\operatorname{ar}(\|\mathsf{gmABQS}) + \operatorname{ar}(\|\mathsf{gmSQCD})]$$

$$\Rightarrow ar(\|gmPQRS) = \frac{1}{2}ar(\|gmABCD)$$

# Question 22:

Given: ABCDE is a pentagon, EG, drawn parallel to DA, meets BA produced at G, and CF, drawn parallel to DB, meets AB produced at F.



To Prove:  $ar(Pentagon ABCDE) = ar(\Delta DGF)$ 

Proof:

Triangles on the same base and between the same parallels are equal in area.

Since  $\Delta {\rm DGA}$  and  $\Delta {\rm AED}$  have same base AD and lie between parallel lines AD and EG

 $\therefore$  ar  $(\Delta DGA) = ar (\Delta AED).....(1)$ 

Similarly,  $\Delta {\rm DBC}$  and  $\Delta {\rm BFD}$  have same baseDB and lie between parallel lines BD and CF.

 $\therefore \quad \operatorname{ar}(\Delta \mathsf{DBF}) = \operatorname{ar}(\Delta \mathsf{DBC})....(2)$ 

Adding both the sides of the equations (1) and (2), we have

 $\therefore$  ar( $\triangle$ DGA)+ ar( $\triangle$ DBF)=ar( $\triangle$ AED)+ar( $\triangle$ BCD)

Adding  $ar(\Delta ABD)$  to both sides, we get,  $ar(\Delta DGA) + ar(\Delta DBF) + ar(\Delta ABD)$ 

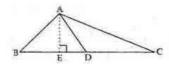
 $= ar(\Delta AED) + ar(\Delta BCD) + ar(\Delta ABD)$ 

... ar (ΔDGA) = ar (pentagon ABCDE)

### Question 23:

Given: ABC is a triangle in which AD is the median.

To Prove:  $ar(\Delta ABD) = ar(\Delta ACD)$ Construction: Draw  $AE \perp BC$ 



Proof; 
$$ar(\Delta ABD) = \frac{1}{2} \times BD \times AE$$

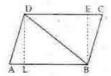
and, 
$$ar(\Delta ADC) = \frac{1}{2} \times DC \times AE$$

Since, 
$$BD = DC$$
 Since D is the median

So, 
$$\operatorname{ar}(\Delta ABD) = \frac{1}{2} \times BD \times AE$$
  
=  $\frac{1}{2} \times DC \times AE = \operatorname{ar}(\Delta ADC)$ 

$$\therefore \quad ar(\Delta ABD) = ar(\Delta ACD)$$

### Quastion 24:



Given: ABCD is a parallelogram in which BD is its diagonal.

To Prove:  $ar(\Delta ABD) = ar(\Delta BCD)$ Construction : Draw DL  $\pm$  AB and BE  $\pm$  CD

Proof: 
$$ar(\Delta ABD) = \frac{1}{2} \times AB \times DL$$
 .....(i

and, 
$$ar(\Delta CBD) = \frac{1}{2} \times CD \times BE$$
 ....(ii)

Now, since ABCD is a parallelogram.

and Ab- CD ....(III

Since distance between two parallel

lines is constant,

$$\Rightarrow \qquad \qquad \mathsf{DL} = \mathsf{BE} \qquad \qquad \ldots .(v)$$

Form (i), (ii), (iii), and (iv) we have

$$ar(\Delta ABD) = \frac{1}{2} \times AB \times DL$$

$$= \frac{1}{2} \times CD \times BE = ar(\Delta CBD)$$

$$ar(\Delta ABD) = ar(\Delta CBD)$$

 $\therefore$  ar( $\triangle$ ABD) = ar(

### Question 25:

Given: A ABC in which D is a point on BC such that;

$$BD = \frac{1}{2}DC$$

To Prove: 
$$ar(\Delta ABD) = \frac{1}{3} ar(\Delta ABC)$$



Construction: Draw AE 

BC

Proof: 
$$ar(\triangle ABD) = \frac{1}{2} \times BD \times AE \dots (1)$$

and, 
$$ar(\Delta ABC) = \frac{1}{2} \times BC \times AE \dots (2)$$

Given that  $BD = \frac{1}{2}BC$ 

So, 
$$BC = BD + DC = BD + 2BD = 3BD$$

$$\therefore BD = \frac{1}{3}BC \qquad ....(3)$$

From (1),

$$ar (\Delta ABD) = \frac{1}{2} \times BD \times AE$$

$$= \frac{1}{2} \times \frac{BC}{3} \times AE$$
 [from (3)]

$$\therefore \operatorname{ar}(\Delta ABD) = \frac{1}{3} \times \left[\frac{1}{2} \times BC \times AE\right]$$
$$= \frac{1}{3} \times \operatorname{ar}(\Delta ABC) \qquad [from (2)]$$

$$\therefore ar(\Delta ABD) = \frac{1}{3} \times ar(\Delta ABC)$$

# Question 26:

```
Given: ABC is a triangle in which D is a point on BC such
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To Prove: 
$$ar(\triangle ABD)$$
:  $ar(\triangle ACD)$   
= m:n

Proof: 
$$ar(\triangle ABD) = \frac{1}{5} \times BD \times BD$$

Proof: 
$$ar(\triangle ABD) = \frac{1}{2} \times BD \times AL$$

and, 
$$ar(\Delta ADC) = \frac{1}{2} \times DC \times AL$$

$$BD = DC \times \frac{m}{n}$$

$$ar(\Delta ABD) = \frac{1}{2} \times BD \times AL$$

$$= \frac{1}{2} \times (DC \times \frac{m}{n}) \times AL$$

$$= \frac{m}{n} \times (\frac{1}{2} \times DC \times AL)$$

$$= \frac{m}{n} \times ar(\Delta ADC)$$

$$\Rightarrow \quad \frac{\text{ar}(\Delta ABD)}{\text{ar}(\Delta ADC)} = \frac{m}{n}$$

$$\Rightarrow$$
 ar( $\triangle$ ABD) : ar( $\triangle$ ADC) = m : n