## CHAPTER 12

## THREE DIMENSIONAL GEOMETRY

## DECEMBER 2020

1. A point R with coordinate 4 lies on the line segment joining the points $\mathrm{P}(2,-3,4)$ and $\mathrm{Q}(8,0,10)$.
a) Find the ratio in which $R$ divides $P Q$.
b) Find the coordinates of $R$

## MARCH 2020

2. Consider the following figure.

a) Find the distance PQ .
b) Find the coordinates of the point divides the line segment joining the points P and Q internally in the ratio $2: 3$.

## IMPROVEMENT 2019

3. a) Origin is the centroid of $\triangle P Q R$ with vertices $P(2 a, 2,6), Q(-4,3 b,-10)$ and $R(8,14,2 c)$ find the values of $\mathrm{a}, \mathrm{b}$ and c .
b) Find length of the values of $\mathrm{a}, \mathrm{b}$ and c .
c) The ratio in which the $Y Z$ plane divides the segment joining the points $(-2,4,7)$

$$
\begin{equation*}
\text { and }(3,-5,8) \text { is } \ldots \ldots \tag{1}
\end{equation*}
$$

## MARCH 2019

4. Let $A(0,7,10), B(-1,6,6)$ and $C(-4,9,6)$ are the vertices of a triangle.
a) Show that it is a right triangle .
b) Find the coordinate of the centre of the circle passing through the points $\mathrm{A}, \mathrm{B}$ and $C$.

## IMPROVEMENT 2018

5. Consider the points $A=(3,8,10)$ and
$B=(6,10,-8)$
a) Find the ratio in which the line segment joining $A$ and $B$ is divided by the YZcoordinate plane.
b) Find the coordinates of the point of division.
c) Which coordinate plane divides the line segment AB internally? Justify your answer.

## MARCH 2018

6. Consider a point $A(4,8,10)$ in space.
a) Find the distance of the point A from XY- plane.
b) Find the distance of the point A from X -axis.
c) Find the ratio in which the line segment joining the point $A$ and $B(6,10,-8)$ is divided by YZ - plane.

## IMPROVEMENT 2017

7. a) Co-ordinates of a point on XY plane is $\qquad$
i) $(1,2,0)$
ii) $(2,-3,-1)$
iii) $(0,3,1)$
iv) $(4,0,1)$
b) Find the ratio in which the XY plane divides the line segment joining the points
$(-2,4,7),(3,-5,8)$.

## MARCH 2017

8. a) The distance between the point $(1,-2,3)$ and $(4,1,2)$ is ......
i) $\sqrt{12}$
ii) $\sqrt{19}$
iii) $\sqrt{11}$
iv) $\sqrt{15}$
b) The centroid of triangle ABC is at the point $(1,2,3)$. If the coordinates of A and B are $(3,-5,7)$ and $(-1,7,-6)$ respectively. Find the coordinates of the point C .

## IMPROVEMENT 2016

9. a) State whether the following is TRUE or

FALSE. " The point $(4,-2,-5)$ lies in the eight octant'.
b) Find the equation of the set of points such that its distance from the points $\mathrm{A}(3,4,-5)$ and B $(-2,1,4)$ are equal.

## MARCH 2016

10. a) Which one of the following points lies in the sixth octant?
i) $(-4,2,-5)$
ii) $(-4,-2,-5)$
iii) $(4,-2,-5)$
iv) $(4,2,5)$
b) Find the ratio in which the YZ plane divides
the line segment formed by joining the points
$(-2,4,7)$ and $(3,-5,8)$

## IMPROVEMENT 2015

11. a) Which of the following is lies in the sixth octant?
i) $(-3,-1,-2)$
ii) $(-3,1,-2)$
iii) $(3,-1,2)$
iv) $(3,-1,-2)$
b) Find the ratio in which the YZ plane divides the line joining the points $(-2,4,7)$ and $(3,-5,8)$.

## MARCH 2015

12. a) A point in the $X Z$ plane is $\qquad$
i) $(1,1,1)$
ii) $(2,0,3)$
iii) $(2,3,0)$
iv) $(-1,2,3)$
b) Show that the points $A(1,2,3), B(-1,-2,-1), C(2,3,2)$ and $D(4,7,6)$ are the vertices of a parallelogram.

## IMPROVEMENT 2014

13. Find the coordinates of the point which, divides the line segment joining the points $(-2,3,5)$ and $(1,-4,6)$ in the ratio $2: 3$ internally.

## MARCH 2014

14. a) Find the distance between the points $(2,3,5)$ and (4,3,1).
b) Find the ratio in which the line segment joining the points $\mathrm{A}(4,8,10)$ and $\mathrm{B}(6,10,-8)$ is divided by the XY pane.

## IMPROVEMENT 2013

15. a) If $P$ is a point in YZ-plane, then its $x$ coordinate is $\qquad$
b) Find the ratio in which the YZ-plane divides the line segment formed by joining the points $(-2,4,7)$ and $(3,-5,8)$.

## MARCH 2013

16. a) Find the distance between the points (2,-1,3) and ( $-2,1,3$ ).
b) Find the coordinates of the point which divides the line segment joining the points $(-2,3,5)$ and $(1,-4,6)$ internally in the ratio of 2:3.

## IMPROVEMENT 2012

17. The vertices of $\triangle A B C$ are $A(2,1), B(-3,5)$ and $C(4,5)$
a) Write the co-ordinates of the midpoint of AC.
b) Find the equation of the medial through the vertex $B$.

## MARCH 2012

18. a) If $\left(\frac{5}{3}, \frac{22}{3}, \frac{-22}{3}\right)$ is the centroid of $\triangle \mathrm{PQR}$ with vertices $P(a, 7,-10), Q(1,2 b,-6), R(4,9,3 c)$, find the values of $\mathrm{a}, \mathrm{b}$ and c .
b) Prove that $\triangle \mathrm{PQR}$ is isosceles.

## IMPROVEMENT 2011

19. a) Determine a point on the $x$ axis which is equidistant from the points $(-2,3,5)$ and (1,2,3).
b) If the centroid of the triangle with vertices $(\mathrm{a}, 2,5),(1, \mathrm{~b}, 0)$ and $(-3,-1, \mathrm{c})$ is $(1,2,3)$, then find $a, b$ and $c$.

## MARCH 2011

20. Consider the points A $(-2,3,5)$, $\mathrm{B}(1,2,3)$ and $\mathrm{C}(7,0,-1)$.
a) Using the distance formula. Show that the points $\mathrm{A}, \mathrm{B}$ and C are collinear.
a) Find the ratio in which $B$ divides the line segment AC.

## SEPTEMBER 2010

21. a) Find the co-ordinates of the points which trisect the line segment joining the points $\mathrm{P}(4,0,1)$ and $\mathrm{Q}(2,4,0)$.
b) Find the locus of the set of points P such that the distance from $\mathrm{A}(2,3,4)$ is equal to twice the distance from $\mathrm{B}(-2,1,2)$.

## MARCH 2010

22. Consider the triangle with vertices A $(0,7,-10)$, $\mathrm{B}(1,6,-6), \mathrm{C}(4,9,-6)$.
i) Find the sides $\mathrm{AB}, \mathrm{BC}, \mathrm{AC}$
ii) Prove that the triangle is right angled.
iii) Find the centroid of the triangle.

## IMPROVEMENT 2009

23. Consider the points $\mathrm{A}(-2,4,7)$ and $\mathrm{B}(3,-5,8)$.
i) If P divides AB in the ratio $\mathrm{k}: 1$, then find the co-ordinates of $P$.
ii) Find the co-ordinates of the point where the line segment AB crosses the YZ -plane.

## MARCH 2009

24. Consider the points $\mathrm{A}(2,1,3)$ and $\mathrm{B}(1,2,1)$ :
a) Find the ratio in which the join of $A B$ is dived by YZ plane.
b) Also find the point of division.

