

EXERCISE 5A PAGE: 90

#### 1. Write each of the following in power notation:

i.  $(5/7) \times (5/7) \times (5/7) \times (5/7)$ 

Solution:-

The product of rational number multiplied several times by itself can be expressed in the power notations as,  $(5/7)^4$ 

ii.  $(-4/3) \times (-4/3) \times (-4/3) \times (-4/3) \times (-4/3)$ 

Solution:-

The product of rational number multiplied several times by itself can be expressed in the power notations as,  $(-4/3)^5$ 

iii.  $(-1/6) \times (-1/6) \times (-1/6)$ 

Solution:-

The product of rational number multiplied several times by itself can be expressed in the power notations as,

 $(-1/6)^3$ 

iv.  $(-8) \times (-8) \times (-8) \times (-8) \times (-8)$ 

Solution:-

The product of rational number multiplied several times by itself can be expressed in the power notations as,

 $(-8)^5$ 

### 2. Express each of the following in power notation:

i. (25/36)

Solution:-

We have,

$$25 = 5 \times 5 = (5)^2$$

$$36 = 6 \times 6 = (6)^2$$

Then,

= 
$$(5^2/6^2)$$
  
  $\therefore (5/6)^2$ 

ii. (-27/64)

Solution:-

We have,

$$-27 = -3 \times -3 \times -3 = (-3)^3$$
  
64 = 4 × 4 × 4 = (4)<sup>3</sup>

Then,



= 
$$(-3^3/4^3)$$
  
 $\therefore (-3/4)^3$ 

### iii. (-32/243)

Solution:-

We have,

$$-32 = -2 \times -2 \times -2 \times -2 \times -2 = (-2)^{5}$$

$$243 = 3 \times 3 \times 3 \times 3 \times 3 = (3)^{5}$$

Then,

= 
$$(-2^5/3^5)$$
  
  $\therefore (-2/3)^5$ 

### iv. (-1/128)

Solution:-

We have,

Then,

= 
$$(-1^7/2^7)$$
  
::  $(-1/2)^7$ 

# 3. Express each of the following a rational number:

i. (2/3)<sup>5</sup>

Solution:-

We have,

$$(2/3)^5 = (2^5/3^5)$$
  
=  $(2 \times 2 \times 2 \times 2 \times 2) / (3 \times 3 \times 3 \times 3 \times 3)$   
=  $(32/243)$ 

ii. (-8/5)<sup>3</sup>

Solution:-

We have,

$$(-8/5)^3 = (-8^3/5^3)$$
  
=  $(-8 \times -8 \times -8) / (5 \times 5 \times 5)$   
=  $(-512/125)$ 

## iii. (-13/11)<sup>2</sup>

Solution:-

We have,

$$(-13/11)^2 = (-13^2/11^2)$$
  
=  $(-13 \times -13) / (11 \times 11)$   
=  $(169/121)$ 



### iv. $(1/6)^3$

#### Solution:-

We have,

$$(1/6)^3 = (1^3/6^3)$$
  
=  $(1 \times 1 \times 1) / (6 \times 6 \times 6)$   
=  $(1/216)$ 

## v. (-1/2)<sup>5</sup>

### Solution:-

We have,

$$(-1/2)^5 = (-1^5/2^5)$$
  
=  $(-1 \times -1 \times -1 \times -1 \times -1) / (2 \times 2 \times 2 \times 2 \times 2)$   
=  $(-1/32)$ 

### vi. $(-4/7)^3$

### Solution:-

We have,

$$(-4/7)^3 = (-4^3/7^3)$$
  
=  $(-4 \times -4 \times -4) / (7 \times 7 \times 7)$   
=  $(-64/343)$ 

## vii. (-1)<sup>9</sup>

#### Solution:-

We have,

## 4. Express each of the following as a rational number:

### i. (4)-1

### Solution:-

We have:

$$(4)^{-1} = (4/1)^{-1}$$
  
=  $(1/4)^{1}$  ... [:  $(a/b)^{-n} = (b/a)^{n}$ ]  
=  $(1/4)$ 

# ii. (-6)<sup>-1</sup>

#### Solution:-

We have:

$$(-6)^{-1} = (-6/1)^{-1}$$
  
=  $(1/-6)^1$  ... [:  $(a/b)^{-n} = (b/a)^n$ ]  
=  $(-1/6)$ 



### iii. (1/3)<sup>-1</sup>

#### Solution:-

We have:

$$(1/3)^{-1} = (-6/1)^{-1}$$
  
=  $(3/1)^{1}$   
= 3

... [: 
$$(a/b)^{-n} = (b/a)^{n}$$
]

### iv. (--2/3)<sup>-1</sup>

#### Solution:-

We have:

$$(-2/3)^{-1} = (-2/3)^{-1}$$
  
=  $(3/-2)^{1}$   
=  $(-3/2)$ 

... [: 
$$(a/b)^{-n} = (b/a)^{n}$$
]

### 5. Find the reciprocal of each of the following:

#### i. (3/8)<sup>4</sup>

Solution:-

We know that the reciprocal of  $(a/b)^m$  is  $(b/a)^m$ Then,

Reciprocal of (3/8)<sup>4</sup> is (8/3)<sup>4</sup>

### ii. (-5/6)<sup>11</sup>

Solution:-

We know that the reciprocal of (a/b) m is (b/a) m

Then,

Reciprocal of  $(-5/6)^{11}$  is  $(-6/5)^{11}$ 

### iii. (6)<sup>7</sup>

Solution:-

We know that the reciprocal of  $(a/b)^m$  is  $(b/a)^m$ 

Then,

Reciprocal of  $(6)^7$  is  $(1/6)^7$ 

### iv. (-4)<sup>3</sup>

#### Solution:-

We know that the reciprocal of  $(a/b)^m$  is  $(b/a)^m$ 

Then

Reciprocal of  $(-4)^3$  is  $(-1/4)^3$ 

# 6. Find the value of each of the following:

i. 8º

Solution:-

By definition, we have  $a^0 = 1$  for every integer.



$$...80 = 1$$

#### $(-3)^0$ ii.

#### Solution:-

By definition, we have  $a^0 = 1$  for every integer.

$$(-3)^0 = 1$$

#### $4^0 + 5^0$ iii.

#### Solution:-

By definition, we have  $a^0 = 1$  for every integer.

$$4^{\circ} + 5^{\circ}$$

= 2

#### $6^{\circ} \times 7^{\circ}$ iv.

#### Solution:-

By definition, we have  $a^0 = 1$  for every integer.

$$\therefore 6^{\circ} \times 7^{\circ}$$

$$= 1 \times 1$$

= 1

### 7. Simplify each of the following and express each as a rational number:

$$(3/2)^4 \times (1/5)^2$$

### Solution:-

We have,

$$(3^4/2^4) = (3\times3\times3\times3)/(2\times2\times2\times2) = (81/16)$$
  
 $(1^2/5^2) = (1\times1)/(5\times5) = (1/25)$ 

Then,

$$=(81/16)\times(1/25)$$

=(81/400)

#### $(-2/3)^5 \times (-3/7)^3$ ii.

#### Solution:-

We have,

$$(-2^5/3^5) = (-2 \times -2 \times -2 \times -2 \times -2)/(3 \times 3 \times 3 \times 3 \times 3) = (-32/243)$$
  
 $(-3^3/7^3) = (-3 \times -3 \times -3)/(7 \times 7 \times 7) = (-27/343)$ 

Then,

$$= (-32/243) \times (-27/343)$$
  
=  $(-32 \times -27) / (243 \times 343)$ 

By simplifying,  
= 
$$(-32\times-1) / (9/343)$$

=(32/3087)



#### iii. $(-1/2)^5 \times 2^3 \times (3/4)^2$

#### Solution:-

We have,

$$(-1^5/2^5) = (-1 \times -1 \times -1 \times -1) / (2 \times 2 \times 2 \times 2 \times 2) = (-1/32)$$
  
 $(2)^3 = (2 \times 2 \times 2) = 8$   
 $(3^2/4^2) = (3 \times 3) / (4 \times 4) = (9/16)$ 

Then,

$$= (-1/32) \times 8 \times (9/16)$$
  
=  $(-1\times8\times9) / (32\times1\times16)$ 

By simplifying,

$$= (-1 \times 1 \times 9) / (32 \times 1 \times 2)$$
  
=  $(-9/64)$ 

## iv. $(2/3)^2 \times (-3/5)^3 \times (7/2)^2$

#### Solution:-

We have,

$$(2^2/3^2) = (2\times2)/(3\times3) = (4/9)$$
  
 $(-3/5)^3 = (-3\times-3\times-3)/(5\times5\times5) = (-27/125)$   
 $(7^2/2^2) = (7\times7)/(2\times2) = (49/4)$ 

Then,

On simplifying,

#### v. $\{(-3/4)^3 - (-5/2)^3\} \times 4^2$

#### Solution:-

We have,

$$= \{(-3^3/4^3) - (5^3/2^3)\} \times 16$$
$$= \{(-27/64) - (-125/8)\} \times 16$$

First we find the difference of {(-27/64)-(125/8)}

LCM of 64 and 8 is 64

#### 8. Simplify and express each as a rational number:

i. 
$$(4/9)^6 \times (4/9)^{-4}$$



#### Solution:-

We have,

$$= (4/9)^{(6+(-4))}$$

$$= (4/9)^{(6-4)}$$

$$= (4/9)^{2}$$

$$= (4^{2}/9^{2})$$

=(16/81)

... 
$$[{(a/b)^m \times (a/b)^n}] = (a/b)^{m-n}$$

ii.  $(-7/8)^{-3} \times (-7/8)^2$ 

Solution:-

We have,

$$= (-7/8)^{(-3+2)}$$

$$= (-7/8)^{(-1)}$$

$$= (-8/7)$$

... 
$$[{(a/b)^m \times (a/b)^n}] = (a/b)^{m-n}$$

iii. (4/3)<sup>-3</sup>× (4/3)<sup>-2</sup>

Solution:-

We have,

$$= (4/3)^{(-3+(-2))}$$

$$= (4/3)^{(-3-2)}$$

$$= (4/3)^{-5}$$

$$= (3/4)^{5}$$

$$= (3^{5}/4^{5})$$

$$= 243/1024$$

... 
$$[{(a/b)^m \times (a/b)^n}] = (a/b)^{m-n}$$

9. Express each of the following as a rational number:

i. 5<sup>-3</sup>

Solution:-

We know that,

$$= (5)^{-3} = (1/5)^3$$
$$= (1^3/5^3)$$
$$= (1/125)$$

... [:: 
$$(a/b)^{-n} = (b/a)^{n}$$
]

ii. (-2)<sup>-5</sup>

Solution:-

We know that,

= 
$$(-2)^{-5}$$
 =  $(-1/2)^3$   
=  $(-1^3/2^3)$   
=  $(-1/8)$ 

... [: 
$$(a/b)^{-n} = (b/a)^{n}$$
]

iii. (1/4)<sup>-4</sup>

Solution:-

We know that,



$$= (1/4)^{-4} = (4/1)^4$$
$$= (4^4/1^4)$$
$$= (256/1)$$
$$= 256$$

... [: 
$$(a/b)^{-n} = (b/a)^{n}$$
]

#### $(-3/4)^{-3}$ iv.

#### Solution:-

We know that,

$$= (-3/4)^{-3} = (-4/3)^3$$
$$= (-4^3/3^3)$$
$$= (-64/27)$$

... [: 
$$(a/b)^{-n} = (b/a)^{n}$$
]

#### $(-3)^{-1} \times (1/3)^{-1}$ ٧.

#### Solution:-

We know that,

$$= (-3)^{-1} = (-1/3)^{1}$$

$$= (1/3)^{-1} = (3/1)^{1}$$

$$= (-1/3) \times (3/1)$$

$$= (-1\times3)/(3\times1)$$

$$= (-3/3)$$

$$= -1$$

... [: 
$$(a/b)^{-n} = (b/a)^{n}$$
]  
... [:  $(a/b)^{-n} = (b/a)^{n}$ ]

#### $(5/7)^{-1} \times (7/4)^{-1}$ vi.

# Solution:-

We know that,

$$= (5/7)^{-1} = (7/5)^{1}$$

$$= (7/4)^{-1} = (4/7)^{1}$$

$$= (7/5) \times (4/7)$$

$$= (7\times4)/(5\times7)$$

... 
$$[\because (a/b)^{-n} = (b/a)^n]$$
  
...  $[\because (a/b)^{-n} = (b/a)^n]$ 

On simplifying,

$$= (1 \times 4) / (5 \times 1)$$
  
= 4/5

#### (5-1-7-1)-1 vii.

#### Solution:-

We know that,

$$= (5)^{-1} = (1/5)^{1}$$

$$= (7)^{-1} = (1/7)^{1}$$
Now subtract,
$$= \{(1/5) - (1/7)\}^{-1}$$

... 
$$[\because (a/b)^{-n} = (b/a)^n]$$
  
...  $[\because (a/b)^{-n} = (b/a)^n]$ 

$$= \{(1/5) - (1/7)\}^{-1}$$

$$= \{(7-5)/35\}^{-1}$$

$$= \{2/35\}^{-1}$$

$$= \{35/2\}$$



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# viii. $\{(4/3)^{-1} - (1/4)^{-1}\}^{-1}$

### Solution:-

We know that,

= 
$$(4/3)^{-1}$$
=  $(3/4)^1$   
=  $(1/4)^{-1}$  =  $(4/1)^1$ 

Now subtract,

$$= \{(3/4) - (4/1)\}^{-1}$$

$$= \{(3-16)/4\}^{-1}$$

$$= \{-13/4\}^{-1}$$

$$= \{-4/13\}$$

... 
$$[\because (a/b)^{-n} = (b/a)^{n}]$$
  
...  $[\because (a/b)^{-n} = (b/a)^{n}]$ 

... [LCM of 4 and 1 is 4]

ix. 
$$\{(3/2)^{-1} \div (-2/5)^{-1}\}$$

#### Solution:-

We know that,

= 
$$(3/2)^{-1}$$
=  $(2/3)^1$   
=  $(-2/5)^{-1}$  =  $(-5/2)^1$ 

Now divide,

$$= \{(2/3) \div (-5/2)\}^{-1}$$

$$= \{(2/3) \times (-2/5)\}$$

$$= \{(2\times -2) / (3\times 5)\}$$

$$= \{-4/15\}$$

... 
$$[\because (a/b)^{-n} = (b/a)^n]$$
  
...  $[\because (a/b)^{-n} = (b/a)^n]$ 

## x. (23/25)<sup>0</sup>

### Solution:-

$$=(23/25)^0=1$$

Because, by definition, we have  $a^0 = 1$  for every integer.



EXERCISE 5B PAGE: 92

#### 1. Express each of the following numbers in standard form:

#### i. 538

#### Solution:-

A given number is said to be in standard form if it can be expressed as  $k \times 10^n$ , where k is a real number such that  $1 \le k < 10$  and n is a positive integer.

Then,

 $538 = 5.38 \times 10^2$ 

#### ii. 6428000

#### Solution:-

A given number is said to be in standard form if it can be expressed as  $k \times 10^n$ , where k is a real number such that  $1 \le k < 10$  and n is a positive integer.

Then,

 $6428000 = 6.428 \times 10^6$ 

#### iii. 82934000000

#### Solution:-

A given number is said to be in standard form if it can be expressed as  $k \times 10^n$ , where k is a real number such that  $1 \le k < 10$  and n is a positive integer.

Then,

 $82934000000 = 8.2934 \times 10^{10}$ 

#### iv. 94000000000

#### Solution:-

A given number is said to be in standard form if it can be expressed as  $k \times 10^n$ , where k is a real number such that  $1 \le k < 10$  and n is a positive integer.

Then

 $9400000000000 = 9.4 \times 10^{11}$ 

#### v. 23000000

#### Solution:-

A given number is said to be in standard form if it can be expressed as  $k \times 10^n$ , where k is a real number such that  $1 \le k < 10$  and n is a positive integer.

Then,

 $23000000 = 2.3 \times 10^7$ 

#### 2. Express each of the following numbers in standard form:

#### i. Diameter of Earth = 12756000 m

#### Solution:-

A given number is said to be in standard form if it can be expressed as  $k \times 10^n$ , where k is a real number such that  $1 \le k < 10$  and n is a positive integer.



Then,

Diameter of Earth = 12756000 m

 $= (1.2156 \times 10^7) \text{ m}$ 

(in standard form)

# ii. Distance between Earth and Moon = 384000000 m Solution:-

A given number is said to be in standard form if it can be expressed as  $k \times 10^n$ , where k is a real number such that  $1 \le k < 10$  and n is a positive integer.

Then,

Distance between Earth and Moon = 384000000 m

 $= (3.84 \times 10^8) \text{ m}$ 

(in standard form)

# iii. Population of India in March 2001= 1027000000 Solution:-

A given number is said to be in standard form if it can be expressed as  $k \times 10^n$ , where k is a real number such that  $1 \le k < 10$  and n is a positive integer.

Then.

Population of India in March 2001= 1027000000

 $= (1.027 \times 10^9)$ 

(in standard form)

# iv. Number of stars in a galaxy = 100000000000 Solution:-

A given number is said to be in standard form if it can be expressed as  $k \times 10^n$ , where k is a real number such that  $1 \le k < 10$  and n is a positive integer.

Then

Number of stars in a galaxy = 100000000000

 $= (1 \times 10^{11})$ 

(in standard form)

# v. The present age of universe = 12000000000 years Solution:-

A given number is said to be in standard form if it can be expressed as  $k \times 10^n$ , where k is a real number such that  $1 \le k < 10$  and n is a positive integer.

Then,

The present age of universe = 12000000000

 $= (1.2 \times 10^{10})$  years

(in standard form)



# EXERCISE 5C PAGE: 93

## Mark tick against the correct answer in each of the following:

- 1.  $(6^{-1}-8^{-1})^{-1}=?$ 
  - (a) (-1/2) Solution:-
- (b)-2
- (c)(1/24)
- (d) 24

(D) 24

We know that,

$$= (6)^{-1} = (1/6)^{1}$$
  
=  $(8)^{-1} = (1/8)^{1}$ 

$$= \{(1/6) - (1/8)\}^{-1}$$
$$= \{(4-3)/24\}^{-1}$$

$$= \{1/24\}^{-1}$$

- = {24/1}
- = 24

- ...  $[\because (a/b)^{-n} = (b/a)^n]$ ...  $[\because (a/b)^{-n} = (b/a)^n]$

... [LCM of 6 and 8 is 24]

... [:  $(a/b)^{-n} = (b/a)^{n}$ ]

... [:  $(a/b)^{-n} = (b/a)^{n}$ ]

- 2.  $(5^{-1} \times 3^{-1})^{-1}$ 
  - (a)(1/15)
- (b)(-1/15)
- (c) 15
- (d)-15

Solution:-

(c) 15

We know that,

$$= (5)^{-1} = (1/5)^{1}$$

$$= (3)^{-1} = (1/3)^{1}$$

$$= \{(1/5) \times (1/3)\}^{-1}$$

$$= \{(1\times1)/(5\times3)\}^{-1}$$

$$= \{1/15\}^{-1}$$

- 3.  $(2^{-1} 4^{-1})^2$ 
  - (a) 4
- (b)-4
- (c) (1/16)

(d) (-1/16)

Solution:-

(c) (1/16)

We know that,

$$= (2)^{-1} = (1/2)^{1}$$

$$= (4)^{-1} = (1/4)^{1}$$

$$= \{(1/2) - (1/4)\}^2$$

$$= \{(2-1)/4\}^2$$

$$= \{1/4\}^2$$

$$= \{1^2/4^2\}$$

... [:  $(a/b)^{-n} = (b/a)^{n}$ ]

... [: 
$$(a/b)^{-n} = (b/a)^{n}$$
]

... [LCM of 2 and 4 is 4]



$$= \{1/16\}$$

4.  $(1/2)^{-2} + (1/3)^{-2} + (1/4)^{-2} = ?$ (a)(61/144) (b) 29

Solution:-

(b) 29

We know that,

$$= (1/2)^{-2} = (2/1)^{2}$$

$$= (1/3)^{-2} = (3/1)^{2}$$

$$= (1/4)^{-2} = (4/1)^{2}$$

Now add,

$$= (2)^{2} + (3)^{2} + (4)^{2}$$
$$= 4 + 9 + 16$$
$$= 29$$

5.  $\{6^{-1}+(3/2)^{-1}\}^{-1}$ 

(a)(2/3)

(b)(5/6)

Solution:-

(c)(6/5)

We know that,

= 
$$(6)^{-1}$$
=  $(1/6)$   
=  $(3/2)^{-1}$  =  $(2/3)$ 

Now add,

$$= \{(1/6) + (2/3)\}^{-1}$$

$$= \{(1+4)/6\}^{-1}$$

$$= \{5/6\}^{-1}$$

$$= \{6/5\}$$

(c) (144/61)

(d) none of these

... [: 
$$(a/b)^{-n} = (b/a)^{n}$$
]

... 
$$[\because (a/b)^{-n} = (b/a)^n]$$

... [: 
$$(a/b)^{-n} = (b/a)^{n}$$
]

(c)(6/5)(d) None of these

... 
$$[\because (a/b)^{-n} = (b/a)^{n}]$$

... 
$$[\because (a/b)^{-n} = (b/a)^n]$$

... [LCM of 6 and 3 is 6]

6.  $(-1/2)^{-6} = ?$ 

(a)-64

(b) 64

(c) (1/64)

(d) (-1/64)

Solution:-(b) 64

We know that,

$$= (-1/2)^{-6} = (-2/1)^{6}$$
$$= (-2)^{6}$$
$$= 64$$

... [:  $(a/b)^{-n} = (b/a)^{n}$ ]

7.  $\{(3/4)^{-1} - (1/4)^{-1}\}^{-1} = ?$ 

(a)(3/8)

(b)(-3/8)

(c)(8/3)

(d)(-8/3)

Solution:-

(b)(-3/8)

We know that,

$$= (3/4)^{-1} = (4/3)^{1}$$

... [:  $(a/b)^{-n} = (b/a)^{n}$ ]



$$= (1/4)^{-1} = (4/1)^{1} \qquad \dots [\because (a/b)^{-n} = (b/a)^{n}]$$
Now subtract,
$$= \{(4/3) - (4/1)\}^{-1}$$

$$= \{(4-12)/3\}^{-1} \qquad \dots [LCM of 3 and 1 is 3]$$

$$= \{-8/3\}^{-1}$$

$$= \{-3/8\}$$

- 8.  $[\{(-1/2)^2\}^{-2}]^{-1}=?$ 
  - (a) (1/16) Solution:-
- (b)16
- (c)(-1/16)
- (d)-16

 $[\{(-1/2)^2\}^{-2}]^{-1} = [\{(-1^2/2^2)\}^{-2}]^{-1}$  $= [\{1/4\}^{-2}]^{-1}$  $= [\{4\}^2]^{-1}$ 

- $= [{4}]^{2}^{-1}$  $= [16]^{-1}$ = [1/16]
- 9. (5/6)<sup>0</sup> =? (a) 5/6

- (b) 0
- (c)1
- (d)none of these

Solution:-

$$(5/6)^0 = 1$$

By definition, we have  $a^0 = 1$  for every integer.

- 10. (2/3)<sup>-5</sup>=?
  - (a)(32/243)
- (b)(243/32)
- (c)(-32/243)
- (d)(-243/32)

Solution:-  $(2/3)^{-5}=(3/2)^5$   $=(3^5/2^5)$ =(243/32)