

EXERCISE 6A

PAGE: 99

1. Add the following expressions:

i. $5x, 7x, -6x$

Solution:-

In the above questions terms having the same literal factors are like terms.

Now add the like terms,

$$= 5x + 7x + (-6x) \quad \dots [\because + \times - = -]$$

Add terms having same sign first,

$$= 5x + 7x - 6x$$

$$= 12x - 6x$$

$$= 6x$$

ii. $(\frac{3}{5})x, (\frac{2}{3})x, (-\frac{4}{5})x$

Solution:-

In the above questions terms having the same literal factors are like terms.

$$= (\frac{3}{5})x + (\frac{2}{3})x + (-\frac{4}{5})x$$

LCM of 5, 3, and 5 is 15

$$= (9x + 10x - 12x) / 15$$

$$= (19x - 12x) / 15$$

$$= (\frac{7}{15})x$$

iii. $5a^2b, -8a^2b, 7a^2b$

Solution:-

In the above questions terms having the same literal factors are like terms.

Now add the like terms,

$$= 5a^2b - 8a^2b + 7a^2b$$

$$= 12a^2b - 8a^2b$$

$$= 4a^2b$$

iv. $(\frac{3}{4})x^2, 5x^2, -3x^2, -(\frac{1}{4})x^2$

Solution:-

In the above questions terms having the same literal factors are like terms.

Now add the like terms,

$$= (\frac{3}{4})x^2 + 5x^2 - 3x^2 - (\frac{1}{4})x^2$$

$$= (\frac{3}{4})x^2 - (\frac{1}{4})x^2 + 5x^2 - 3x^2$$

$$= ((\frac{3-1}{4})x^2 + 2x^2$$

$$= (\frac{2}{4})x^2 + 2x^2$$

$$= (\frac{1}{2})x^2 + 2x^2$$

$$= ((\frac{1+4}{2})x^2$$

$$= (\frac{5}{2})x^2$$

v. $x - 3y + 4z, y - 2x - 8z, 5x - 2y - 3z$

Solution:-

Required sum,

$$= (x - 3y + 4z) + (y - 2x - 8z) + (5x - 2y - 3z)$$

Collecting like terms,

$$= x - 2x + 5x - 3y + y - 2y + 4z - 8z - 3z$$

Adding like terms,

$$= (1 - 2 + 5)x + (-3 + 1 - 2)y + (4 - 8 - 3)z$$

$$= 4x - 4y - 7z$$

vi. $2x^2 - 3y^2, 5x^2 + 6y^2, -3x^2 - 4y^2$

Solution:-

Required sum,

$$= (2x^2 - 3y^2) + (5x^2 + 6y^2) + (-3x^2 - 4y^2)$$

Collecting like terms,

$$= 2x^2 + 5x^2 - 3x^2 - 3y^2 + 6y^2 - 4y^2$$

Adding like terms,

$$= (2 + 5 - 3)x^2 + (-3 + 6 - 4)y^2$$

$$= 4x^2 - y^2$$

vii. $5x - 2x^2 - 8, 8x^2 - 7x - 9, 3 + 7x^2 - 2x$

Solution:-

Required sum,

$$= (5x - 2x^2 - 8) + (8x^2 - 7x - 9) + (3 + 7x^2 - 2x)$$

Collecting like terms,

$$= 2x^2 + 8x^2 + 7x^2 + 5x - 7x - 2x - 8 - 9 + 3$$

$$= (-2 + 8 + 7)x^2 + (5 - 7 - 2)x + (-8 - 9 + 3)$$

$$= 13x^2 - 4x - 14$$

viii. $(\frac{2}{3})a - (\frac{4}{5})b + (\frac{3}{5})c, -(\frac{3}{4})a - (\frac{5}{2})b + (\frac{2}{3})c, (\frac{5}{2})a + (\frac{7}{4})b - (\frac{5}{6})c$

Solution:-

Required sum,

$$= [(\frac{2}{3})a - (\frac{4}{5})b + (\frac{3}{5})c] + [-(\frac{3}{4})a - (\frac{5}{2})b + (\frac{2}{3})c] + [(\frac{5}{2})a + (\frac{7}{4})b - (\frac{5}{6})c]$$

Collecting like terms,

$$= (\frac{2}{3})a - (\frac{3}{4})a + (\frac{5}{2})a - (\frac{4}{5})b - (\frac{5}{2})b + (\frac{7}{4})b + (\frac{3}{5})c + (\frac{2}{3})c - (\frac{5}{6})c$$

$$= [(\frac{2}{3}) - (\frac{3}{4}) + (\frac{5}{2})]a + [(-\frac{4}{5}) - (\frac{5}{2}) + (\frac{7}{4})]b + [(\frac{3}{5}) + (\frac{2}{3}) - (\frac{5}{6})]c$$

$$= [(\frac{8 - 9 + 30}{12})a] + [(-\frac{16 - 15 + 30}{20})b] + [(\frac{18 + 20 - 25}{30})c]$$

$$= (\frac{29}{12})a + (-\frac{31}{20})b + (\frac{13}{30})c$$

ix. $(\frac{8}{5})x + (\frac{11}{7})y + (\frac{9}{4})xy, (-\frac{3}{2})x - (\frac{5}{3})y - (\frac{9}{5})xy$

Solution:-

Required sum,

$$[(\frac{8}{5})x + (\frac{11}{7})y + (\frac{9}{4})xy] + [(-\frac{3}{2})x - (\frac{5}{3})y - (\frac{9}{5})xy]$$

RS Aggarwal Solutions for Class 7 Maths chapter 6
Algebraic Expressions

Collecting like terms,

$$= [(8/5)x - (3/2)x] + [(11/7)y - (5/3)y] + [(9/4)xy - (9/5)xy]$$

$$= (1/10)x - (2/21)y + (9/20)xy$$

x. $(3/2)x^3 - (1/4)x^2 + (5/3), (-5/4)x^3 + (3/5)x^2 - x + (1/5), -x^2 + (3/8)x - (8/15)$

Solution:-

Required sum,

$$= (3/2)x^3 - (1/4)x^2 + (5/3), (-5/4)x^3 + (3/5)x^2 - x + (1/5), -x^2 + (3/8)x - (8/15)$$

Collecting like terms,

$$= [(3/2)x^3 - (5/4)x^3] + [- (1/4)x^2 + (3/5)x^2 - x^2] + [- x + (3/8)x] + [(5/3) + (1/5) - (8/15)]$$

$$= (1/4)x^3 - (13/20)x^2 - (5/8)x + (4/3)$$

2. Subtract :

i. $-8xy$ from $7xy$

Solution:-

The difference of two like terms is a like term whose coefficient is the difference of the numerical coefficient of the two like terms.

Then,

$$= (7 - (-8))xy$$

$$= 15xy$$

ii. X^2 from $-3x^2$

Solution:-

The difference of two like terms is a like term whose coefficient is the difference of the numerical coefficient of the two like terms.

Then,

$$= (-3 - 1)x^2$$

$$= -4x^2$$

iii. $(x - y)$ from $(4y - 5x)$

Solution:-

The difference of two like terms is a like term whose coefficient is the difference of the numerical coefficient of the two like terms.

We have,

$$= (4y - 5x) - (x - y)$$

Change the sign of each term of the expression to be subtracted and then add.

$$= 4y - 5x - x + y$$

$$= (-5x - x) + (4y + y)$$

$$= -5x + 3y$$

$$= 3y - 5x$$

iv. $(a^2 + b^2 - 2ab)$ from $(a^2 + b^2 + 2ab)$ **Solution:-**

The difference of two like terms is a like term whose coefficient is the difference of the numerical coefficient of the two like terms.

We have,

$$= (a^2 + b^2 + 2ab) - (a^2 + b^2 - 2ab)$$

Change the sign of each term of the expression to be subtracted and then add.

$$\begin{aligned} &= a^2 + b^2 + 2ab - a^2 - b^2 + 2ab \\ &= (1 - 1)a^2 + (1 - 1)b^2 + (2 + 2)ab \\ &= (0)a^2 + (0)b^2 + (4)ab \\ &= 4ab \end{aligned}$$

v. $(x^2 - y^2)$ from $(2x^2 - 3y^2 + 6xy)$ **Solution:-**

The difference of two like terms is a like term whose coefficient is the difference of the numerical coefficient of the two like terms.

We have,

$$= (2x^2 - 3y^2 + 6xy) - (x^2 - y^2)$$

Change the sign of each term of the expression to be subtracted and then add.

$$\begin{aligned} &= 2x^2 - 3y^2 + 6xy - x^2 + y^2 \\ &= (2x^2 - x^2) + (-3y^2 + y^2) + 6xy \\ &= (2 - 1)x^2 + (-3 + 1)y^2 + 6xy \\ &= 1x^2 + (-2y^2) + 6xy \\ &= 1x^2 - 2y^2 + 6xy \end{aligned}$$

vi. $(x - y + 3z)$ from $(2z - x - 3y)$ **Solution:-**

The difference of two like terms is a like term whose coefficient is the difference of the numerical coefficient of the two like terms.

We have,

$$= (2z - x - 3y) - (x - y + 3z)$$

Change the sign of each term of the expression to be subtracted and then add.

$$\begin{aligned} &= 2z - x - 3y - x + y - 3z \\ &= (2z - 3z) + (-x - x) + (-3y + y) \\ &= (2 - 3)z + (-1 - 1)x + (-3 + 1)y \\ &= -1z - 2x - 2y \end{aligned}$$

3. Subtract $(2a - 3b + 4c)$ from the sum of $(a + 3b - 4c)$, $(4a - b + 9c)$ and $(-2b + 3c - a)$ **Solution:-**

First we find the sum of $(a + 3b - 4c)$, $(4a - b + 9c)$ and $(-2b + 3c - a)$

$$\begin{aligned} &= (a + 3b - 4c) + (4a - b + 9c) + (-2b + 3c - a) \\ &= (a + 3b - 4c + 4a - b + 9c - 2b + 3c - a) \\ &= (a + 4a - a) + (3b - b - 2b) + (-4c + 9c + 3c) \end{aligned}$$

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Algebraic Expressions

$$\begin{aligned} &= (1 + 4 - 1)a + (3 - 1 - 2)b + (-4 + 9 + 3)c \\ &= 4a + (0)b + 8c \\ &= 4a + 8c \end{aligned}$$

Then,

Subtract $(2a - 3b + 4c)$ from $(4a + 8c)$

$$\begin{aligned} &= (4a + 8c) - (2a - 3b + 4c) \\ &= 4a + 8c - 2a + 3b - 4c \\ &= (4a - 2a) + (3b) + (8c - 4c) \\ &= 2a + 3b + 4c \end{aligned}$$

EXERCISE 6B

PAGE: 102

Find the products:

1. $3a^2 \times 8a^4$

Solution:-

The coefficient of the product of two monomials is equal to the product of their coefficients.

The variable part in the product of two monomials is equal to the product of the variables in the given monomials.

Then,

$$\begin{aligned}
 &= (3 \times 8) \times (a^2 \times a^4) \\
 &= (24) \times (a^{2+4}) && \dots [\because a^m \times a^n = a^{m+n}] \\
 &= (24) \times (a^6) \\
 &= 24 a^6
 \end{aligned}$$

2. $-6x^3 \times 5x^2$

Solution:-

The coefficient of the product of two monomials is equal to the product of their coefficients.

The variable part in the product of two monomials is equal to the product of the variables in the given monomials.

Then,

$$\begin{aligned}
 &= (-6 \times 5) \times (x^3 \times x^2) \\
 &= (-30) \times (x^{3+2}) && \dots [\because a^m \times a^n = a^{m+n}] \\
 &= (-30) \times (x^5) \\
 &= -30 x^5
 \end{aligned}$$

3. $(-4ab) \times (-3a^2bc)$

Solution:-

The coefficient of the product of two monomials is equal to the product of their coefficients.

The variable part in the product of two monomials is equal to the product of the variables in the given monomials.

Then,

$$\begin{aligned}
 &= (-4 \times -3) \times (a \times a^2) \times (b \times b) \times c \\
 &= (12) \times (a^{1+2}) \times (b^{1+1}) \times c && \dots [\because a^m \times a^n = a^{m+n}] \\
 &= (12) \times (a^3) \times (b^2) \times c \\
 &= 12a^3b^2c
 \end{aligned}$$

4. $(2a^2b^3) \times (-3a^3b)$

Solution:-

The coefficient of the product of two monomials is equal to the product of their coefficients.

The variable part in the product of two monomials is equal to the product of the variables in the given monomials.

Then,

$$= (2 \times -3) \times (a^2 \times a^3) \times (b^3 \times b)$$

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Algebraic Expressions

$$\begin{aligned}
 &= (-6) \times (a^{2+3}) \times (b^{3+1}) && \dots [\because a^m \times a^n = a^{m+n}] \\
 &= (-6) \times (a^5) \times (b^4) \\
 &= -6a^5b^4
 \end{aligned}$$

5. $(\frac{2}{3})x^2y \times (\frac{3}{5})xy^2$

Solution:-

The coefficient of the product of two monomials is equal to the product of their coefficients.

The variable part in the product of two monomials is equal to the product of the variables in the given monomials.

Then,

$$\begin{aligned}
 &= [(\frac{2}{3}) \times (\frac{3}{5})] \times (x^2 \times x) \times (y \times y^2) \\
 &= [(\frac{2 \times 3}{3 \times 5})] \times (x^{2+1}) \times (y^{1+2}) && \dots [\because a^m \times a^n = a^{m+n}] \\
 &= [(\frac{2 \times 1}{1 \times 5})] \times (x^3) \times (y^3) \\
 &= [\frac{2}{5}]x^3y^3
 \end{aligned}$$

6. $(-\frac{3}{4})ab^3 \times (-\frac{2}{3})a^2b^4$

Solution:-

The coefficient of the product of two monomials is equal to the product of their coefficients.

The variable part in the product of two monomials is equal to the product of the variables in the given monomials.

Then,

$$\begin{aligned}
 &= [(-\frac{3}{4}) \times (-\frac{2}{3})] \times (a \times a^2) \times (b^3 \times b^4) \\
 &= [(\frac{-3 \times -2}{4 \times 3})] \times (a^{1+2}) \times (b^{3+4}) && \dots [\because a^m \times a^n = a^{m+n}] \\
 &= [(\frac{-1 \times -1}{2 \times 1})] \times (a^3) \times (b^7) \\
 &= [\frac{1}{2}]a^3b^7
 \end{aligned}$$

7. $(-\frac{1}{27})a^2b^2 \times (-\frac{9}{2})a^3bc^2$

Solution:-

The coefficient of the product of two monomials is equal to the product of their coefficients.

The variable part in the product of two monomials is equal to the product of the variables in the given monomials.

Then,

$$\begin{aligned}
 &= [(-\frac{1}{27}) \times (-\frac{9}{2})] \times (a^2 \times a^3) \times (b^2 \times b) \times c^2 \\
 &= [(\frac{-1 \times -9}{27 \times 2})] \times (a^{2+3}) \times (b^{2+1}) \times c^2 && \dots [\because a^m \times a^n = a^{m+n}] \\
 &= [(\frac{-1 \times -1}{3 \times 2})] \times (a^5) \times (b^3) \times c^2 \\
 &= [\frac{1}{6}]a^5b^3c^2
 \end{aligned}$$

8. $(-\frac{13}{5})ab^2c \times (\frac{7}{3})a^2bc^2$

Solution:-

The coefficient of the product of two monomials is equal to the product of their coefficients.

The variable part in the product of two monomials is equal to the product of the variables in the given monomials.

Then,

$$= [(-\frac{13}{5}) \times (\frac{7}{3})] \times (a \times a^2) \times (b^2 \times b) \times (c \times c^2)$$

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Algebraic Expressions

$$\begin{aligned}
 &= [(-13 \times 7) / (5 \times 3)] \times (a^{1+2}) \times (b^{2+1}) \times (c^{1+2}) && \dots [\because a^m \times a^n = a^{m+n}] \\
 &= [-91 / 15] \times (a^3) \times (b^3) \times c^3 \\
 &= [-91/15]a^3b^3c^3
 \end{aligned}$$

9. $(-18/5)x^2z \times (-25/6)xz^2y$

Solution:-

The coefficient of the product of two monomials is equal to the product of their coefficients.

The variable part in the product of two monomials is equal to the product of the variables in the given monomials.

Then,

$$\begin{aligned}
 &= [(-18/5) \times (-25/6)] \times (x^2 \times x) \times (z \times z^2) \times (y) \\
 &= [(-18 \times -25) / (5 \times 6)] \times (x^{2+1}) \times (z^{1+2}) \times (y) && \dots [\because a^m \times a^n = a^{m+n}] \\
 &= [(-3 \times -5) / (1 \times 1)] \times (x^3) \times (z^3) \times y \\
 &= 15x^3z^3y
 \end{aligned}$$

10. $(-3/14)xy^4 \times (7/6)x^3y$

Solution:-

The coefficient of the product of two monomials is equal to the product of their coefficients.

The variable part in the product of two monomials is equal to the product of the variables in the given monomials.

Then,

$$\begin{aligned}
 &= [(-3/14) \times (7/6)] \times (x \times x^3) \times (y^4 \times y) \\
 &= [(-3 \times 7) / (14 \times 6)] \times (x^{1+3}) \times (y^{4+1}) && \dots [\because a^m \times a^n = a^{m+n}] \\
 &= [(-1 \times 1) / (2 \times 2)] \times (x^4) \times (y^5) \\
 &= (-1/4)x^4y^5
 \end{aligned}$$

11. $(-7/5)x^2y \times (3/2)xy^2 \times (-6/5)x^3y^3$

Solution:-

The coefficient of the product of two monomials is equal to the product of their coefficients.

The variable part in the product of two monomials is equal to the product of the variables in the given monomials.

Then,

$$\begin{aligned}
 &= [(-7/5) \times (3/2) \times (-6/5)] \times (x^2 \times x \times x^3) \times (y \times y^2 \times y^3) \\
 &= [(-7 \times 3 \times -6) / (5 \times 2 \times 5)] \times (x^{2+1+3}) \times (y^{1+2+3}) && \dots [\because a^m \times a^n = a^{m+n}] \\
 &= [(-7 \times 3 \times -2) / (5 \times 1 \times 5)] \times (x^6) \times (y^6) \\
 &= (63/25)x^6y^6
 \end{aligned}$$

12. $2a^2b \times (-5)ab^2c \times (-6)bc^2$

Solution:-

The coefficient of the product of two monomials is equal to the product of their coefficients.

The variable part in the product of two monomials is equal to the product of the variables in the given monomials.

Then,

$$= [(2) \times (-5) \times (-6)] \times (a^2 \times a) \times (b \times b^2 \times b) \times (c \times c^2)$$

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Algebraic Expressions

the following steps

$$\begin{aligned} &= [60] \times (a^{2+1}) \times (b^{1+2+1}) \times (c^{1+2}) \\ &= [60] \times (a^3) \times (b^4) \times (c^3) \\ &= [60]a^3b^4c^3 \end{aligned}$$

$$\dots [\because a^m \times a^n = a^{m+n}]$$

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EXERCISE 6C

PAGE: 104

Find each of the following products:

1. $4a(3a + 7b)$

Solution:-

Let p, q and r be three monomials.

Then, by distributive law of multiplication over addition, we have:

$$P \times (q + r) = (p \times q) + (p \times r)$$

Now,

$$= (4a \times 3a) + (4a \times 7b)$$

$$= (12a^2 + 28ab)$$

$$\dots [\because a^m \times a^n = a^{m+n}]$$

2. $5a(6a - 3b)$

Solution:-

Let p, q and r be three monomials.

Then, by distributive law of multiplication over subtraction, we have:

$$P \times (q - r) = (p \times q) - (p \times r)$$

Now,

$$= (5a \times 6a) - (5a \times 3b)$$

$$= (30a^2 - 15ab)$$

$$\dots [\because a^m \times a^n = a^{m+n}]$$

3. $8a^2(2a + 5b)$

Solution:-

Let p, q and r be three monomials.

Then, by distributive law of multiplication over addition, we have:

$$P \times (q + r) = (p \times q) + (p \times r)$$

Now,

$$= (8a^2 \times 2a) + (8a^2 \times 5b)$$

$$= (16a^3 + 40a^2b)$$

$$\dots [\because a^m \times a^n = a^{m+n}]$$

4. $9x^2(5x + 7)$

Solution:-

Let p, q and r be three monomials.

Then, by distributive law of multiplication over addition, we have:

$$P \times (q + r) = (p \times q) + (p \times r)$$

Now,

$$= (9x^2 \times 5x) + (9x^2 \times 7)$$

$$= (45x^3 + 63x^2)$$

$$\dots [\because a^m \times a^n = a^{m+n}]$$

5. $ab(a^2 - b^2)$

Solution:-

Let p, q and r be three monomials.

Then, by distributive law of multiplication over subtraction, we have:

$$P \times (q - r) = (p \times q) - (p \times r)$$

Now,

$$\begin{aligned} &= (ab \times a^2) - (ab \times b^2) \\ &= (a^3b + ab^3) \end{aligned}$$

$$\dots [\because a^m \times a^n = a^{m+n}]$$

6. $2x^2(3x - 4x^2)$

Solution:-

Let p, q and r be three monomials.

Then, by distributive law of multiplication over subtraction, we have:

$$P \times (q - r) = (p \times q) - (p \times r)$$

Now,

$$\begin{aligned} &= (2x^2 \times 3x) - (2x^2 \times 4x^2) \\ &= (6x^3 - 8x^4) \end{aligned}$$

$$\dots [\because a^m \times a^n = a^{m+n}]$$

7. $(3/5)m^2n(m + 5n)$

Solution:-

Let p, q and r be three monomials.

Then, by distributive law of multiplication over addition, we have:

$$P \times (q + r) = (p \times q) + (p \times r)$$

Now,

$$\begin{aligned} &= ((3/5)m^2n \times m) + ((3/5)m^2n \times 5n) \\ &= ((3/5)m^3n + 3m^2n^2) \end{aligned}$$

$$\dots [\because a^m \times a^n = a^{m+n}]$$

8. $-17x^2(3x - 4)$

Solution:-

Let p, q and r be three monomials.

Then, by distributive law of multiplication over subtraction, we have:

$$P \times (q - r) = (p \times q) - (p \times r)$$

Now,

$$\begin{aligned} &= (-17x^2 \times 3x) - (-17x^2 \times 4) \\ &= (-51x^3 + 68x^2) \end{aligned}$$

$$\dots [\because a^m \times a^n = a^{m+n}]$$

9. $(7/2)x^2((4/7)x + 2)$

Solution:-

Let p, q and r be three monomials.

Then, by distributive law of multiplication over addition, we have:

$$P \times (q + r) = (p \times q) + (p \times r)$$

Now,

$$\begin{aligned} &= ((7/2)x^2 \times (4/7)x) + ((7/2)x^2 \times 2) \\ &= ((7 \times 4)/(2 \times 7))x^3 + ((7 \times 2)/(2 \times 1))x^2 \\ &= ((1 \times 2)/(1 \times 1))x^3 + ((7 \times 1)/(1 \times 1))x^2 \\ &= (2)x^3 + (7)x^2 \end{aligned}$$

$$\dots [\because a^m \times a^n = a^{m+n}]$$

10. $-4x^2y(3x^2 - 5y)$

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Algebraic Expressions

Solution:-

Let p, q and r be three monomials.

Then, by distributive law of multiplication over subtraction, we have:

$$P \times (q - r) = (p \times q) - (p \times r)$$

Now,

$$\begin{aligned} &= (-4x^2y \times 3x^2) - (-4x^2y \times -5y) \\ &= (-12x^4y + 20x^2y^2) \end{aligned}$$

... [$\because a^m \times a^n = a^{m+n}$]

11. $(-4/27)xyz((9/2)x^2yz - (3/4)xyz^2)$ **Solution:-**

Let p, q and r be three monomials.

Then, by distributive law of multiplication over subtraction, we have:

$$P \times (q - r) = (p \times q) - (p \times r)$$

Now,

$$\begin{aligned} &= ((-4/27)xyz \times (9/2)x^2yz) - ((-4/27)xyz \times (-3/4)xyz^2) \\ &= ((-4 \times 9) / (27 \times 2))x^3y^2z^2 + ((-4 \times -3) / (27 \times 4))x^2y^2z^3 \\ &= ((-2 \times 1) / (3 \times 1))x^3y^2z^2 + ((-1 \times -1) / (9 \times 1))x^2y^2z^3 \\ &= (-2/3)x^3y^2z^2 + (1/9)x^2y^2z^3 \end{aligned}$$

... [$\because a^m \times a^n = a^{m+n}$]

12. $9t^2(t + 7t^3)$ **Solution:-**

Let p, q and r be three monomials.

Then, by distributive law of multiplication over addition, we have:

$$P \times (q + r) = (p \times q) + (p \times r)$$

Now,

$$\begin{aligned} &= (9t^2 \times t) + (9t^2 \times 7t^3) \\ &= (9t^3 + 63t^5) \end{aligned}$$

... [$\because a^m \times a^n = a^{m+n}$]

13. $10a^2(0.1a - 0.5b)$ **Solution:-**

Let p, q and r be three monomials.

Then, by distributive law of multiplication over subtraction, we have:

$$P \times (q - r) = (p \times q) - (p \times r)$$

Now,

$$\begin{aligned} &= (10a^2 \times 0.1a) - (10a^2 \times 0.5b) \\ &= (1a^3 - 5a^2b) \end{aligned}$$

... [$\because a^m \times a^n = a^{m+n}$]

EXERCISE 6D

PAGE: 106

Find each of the following products:

1. $(5x + 7)(3x + 4)$

Solution:-

Suppose $(a + b)$ and $(c + d)$ are two binomials. By using the distributive law of multiplication over addition twice, we may find their product as given below.

$$(a + b) \times (c + d) = a \times (c + d) + b \times (c + d) = (a \times c + a \times d) + (b \times c + b \times d) \\ = ac + ad + bc + bd$$

Let,

$$a = 5x, b = 7, c = 3x, d = 4$$

Now,

$$= 5x \times (3x + 4) + 7 \times (3x + 4) \\ = [(5x \times 3x) + (5x \times 4)] + [(7 \times 3x) + (7 \times 4)] \\ = [15x^2 + 20x + 21x + 28] \\ = [15x^2 + 41x + 28]$$

2. $(4x - 3)(2x + 5)$

Solution:-

Suppose $(a - b)$ and $(c + d)$ are two binomials. By using the distributive law of multiplication over addition twice, we may find their product as given below.

$$(a - b) \times (c + d) = a \times (c + d) - b \times (c + d) = (a \times c + a \times d) - (b \times c + b \times d) \\ = ac + ad - bc - bd$$

Let,

$$a = 4x, b = 3, c = 2x, d = 5$$

Now,

$$= 4x \times (2x + 5) - 3 \times (2x + 5) \\ = [(4x \times 2x) + (4x \times 5)] - [(3 \times 2x) + (3 \times 5)] \\ = [8x^2 + 20x - 6x - 15] \\ = [8x^2 + 14x - 15]$$

3. $(x - 6)(4x + 9)$

Solution:-

Suppose $(a - b)$ and $(c + d)$ are two binomials. By using the distributive law of multiplication over addition twice, we may find their product as given below.

$$(a - b) \times (c + d) = a \times (c + d) - b \times (c + d) = (a \times c + a \times d) - (b \times c + b \times d) \\ = ac + ad - bc - bd$$

Let,

$$a = x, b = 6, c = 4x, d = 9$$

Now,

$$= x \times (4x + 9) - 6 \times (4x + 9) \\ = [(x \times 4x) + (x \times 9)] - [(6 \times 4x) + (6 \times 9)] \\ = [4x^2 + 9x - 24x - 54]$$

$$= [4x^2 - 15x - 54]$$

4. $(5y - 1)(3y - 8)$

Solution:-

Suppose $(a - b)$ and $(c - d)$ are two binomials. By using the distributive law of multiplication over addition twice, we may find their product as given below.

$$\begin{aligned}(a - b) \times (c - d) &= a \times (c - d) - b \times (c - d) = (a \times c - a \times d) - (b \times c - b \times d) \\ &= ac - ad - bc + bd\end{aligned}$$

Let,

$$a = 5y, b = 1, c = 3y, d = 8$$

Now,

$$\begin{aligned}&= 5y \times (3y - 8) - 1 \times (3y - 8) \\ &= [(5y \times 3y) + (5y \times -8)] - [(1 \times 3y) + (1 \times -8)] \\ &= [15y^2 - 40y - 3y + 8] \\ &= [15y^2 - 43y + 8]\end{aligned}$$

5. $(7x + 2y)(x + 4y)$

Solution:-

Suppose $(a + b)$ and $(c + d)$ are two binomials. By using the distributive law of multiplication over addition twice, we may find their product as given below.

$$\begin{aligned}(a + b) \times (c + d) &= a \times (c + d) + b \times (c + d) = (a \times c + a \times d) + (b \times c + b \times d) \\ &= ac + ad + bc + bd\end{aligned}$$

Let,

$$a = 7x, b = 2y, c = x, d = 4y$$

Now,

$$\begin{aligned}&= 7x \times (x + 4y) + 2y \times (x + 4y) \\ &= [(7x \times x) + (7x \times 4y)] + [(2y \times x) + (2y \times 4y)] \\ &= [7x^2 + 28xy + 2yx + 8y^2] \\ &= [7x^2 + 30xy + 8y^2]\end{aligned}$$

6. $(9x + 5y)(4x + 3y)$

Solution:-

Suppose $(a + b)$ and $(c + d)$ are two binomials. By using the distributive law of multiplication over addition twice, we may find their product as given below.

$$\begin{aligned}(a + b) \times (c + d) &= a \times (c + d) + b \times (c + d) = (a \times c + a \times d) + (b \times c + b \times d) \\ &= ac + ad + bc + bd\end{aligned}$$

Let,

$$a = 9x, b = 5y, c = 4x, d = 3y$$

Now,

$$\begin{aligned}&= 9x \times (4x + 3y) + 5y \times (4x + 3y) \\ &= [(9x \times 4x) + (9x \times 3y)] + [(5y \times 4x) + (5y \times 3y)] \\ &= [36x^2 + 27xy + 20yx + 15y^2] \\ &= [36x^2 + 47xy + 15y^2]\end{aligned}$$

7. $(3m - 4n)(2m - 3n)$ **Solution:-**

Suppose $(a - b)$ and $(c - d)$ are two binomials. By using the distributive law of multiplication over addition twice, we may find their product as given below.

$$(a - b) \times (c - d) = a \times (c - d) - b \times (c - d) = (a \times c - a \times d) - (b \times c - b \times d) \\ = ac - ad - bc + bd$$

Let,

$$a = 3m, b = 4n, c = 2m, d = 3n$$

Now,

$$= 3m \times (2m - 3n) - 4n \times (2m - 3n) \\ = [(3m \times 2m) + (3m \times -3n)] - [(4n \times 2m) + (4n \times -3n)] \\ = [6m^2 - 9mn - 8mn + 12n^2] \\ = [6m^2 - 17mn + 12n^2]$$

8. $(0.8x - 0.5y)(1.5x - 3y)$ **Solution:-**

Suppose $(a - b)$ and $(c - d)$ are two binomials. By using the distributive law of multiplication over addition twice, we may find their product as given below.

$$(a - b) \times (c - d) = a \times (c - d) - b \times (c - d) = (a \times c - a \times d) - (b \times c - b \times d) \\ = ac - ad - bc + bd$$

Let,

$$a = 0.8x, b = 0.5y, c = 1.5x, d = 3y$$

Now,

$$= 0.8x \times (1.5x - 3y) - 0.5y \times (1.5x - 3y) \\ = [(0.8x \times 1.5x) + (0.8x \times -3y)] - [(0.5y \times 1.5x) + (0.5y \times -3y)] \\ = [1.2x^2 - 2.4xy - 0.75yx + 1.5y^2] \\ = [1.2x^2 - 3.15xy + 1.5y^2]$$

9. $((1/5)x + 2y)((2/3)x - y)$ **Solution:-**

Suppose $(a + b)$ and $(c - d)$ are two binomials. By using the distributive law of multiplication over addition twice, we may find their product as given below.

$$(a + b) \times (c - d) = a \times (c - d) + b \times (c - d) = (a \times c - a \times d) + (b \times c - b \times d) \\ = ac - ad + bc - bd$$

Let,

$$a = (1/5)x, b = 2y, c = (2/3)x, d = y$$

Now,

$$= (1/5)x \times ((2/3)x - y) + 2y \times ((2/3)x - y) \\ = [((1/5)x \times (2/3)x) + ((1/5)x \times -y)] + [(2y \times (2/3)x) + (2y \times -y)] \\ = [(2/15)x^2 - (1/5)xy + (4/3)yx - 2y^2] \\ = [(2/15)x^2 + (17/15)xy - 2y^2]$$

10. $((2/5)x - (1/2)y)(10x - 8y)$ **Solution:-**

Suppose $(a - b)$ and $(c - d)$ are two binomials. By using the distributive law of multiplication over addition twice, we may find their product as given below.

$$(a - b) \times (c - d) = a \times (c - d) - b \times (c - d) = (a \times c - a \times d) - (b \times c - b \times d) \\ = ac - ad - bc + bd$$

Let,

$$a = (2/5)x, b = (1/2)y, c = 10x, d = 8y$$

Now,

$$= (2/5)x \times (10x - 8y) - (1/2)y \times (10x - 8y) \\ = [(2/5)x \times 10x + (2/5)x \times -8y] - [(1/2)y \times 10x + (1/2)y \times -8y] \\ = [4x^2 - (16/5)xy - 5yx + 4y^2] \\ = [4x^2 - (41/5)xy + 4y^2]$$

11. $((3/4)a + (2/3)b)(4a + 3b)$ **Solution:-**

Suppose $(a + b)$ and $(c + d)$ are two binomials. By using the distributive law of multiplication over addition twice, we may find their product as given below.

$$(a + b) \times (c + d) = a \times (c + d) + b \times (c + d) = (a \times c + a \times d) + (b \times c + b \times d) \\ = ac + ad + bc + bd$$

Let,

$$a = (3/4)a, b = (2/3)b, c = 4a, d = 3b$$

Now,

$$= (3/4)a \times (4a + 3b) + (2/3)b \times (4a + 3b) \\ = [(3/4)a \times 4a + (3/4)a \times 3b] + [(2/3)b \times 4a + (2/3)b \times 3b] \\ = [3a^2 + (9/4)ab + (8/3)ab + 2b^2] \\ = [3a^2 + ((27+32)/12)ab + 2b^2] \\ = [3a^2 + (59/12)ab + 2b^2]$$

12. $(x^2 - a^2)(x - a)$ **Solution:-**

Suppose $(a - b)$ and $(c - d)$ are two binomials. By using the distributive law of multiplication over addition twice, we may find their product as given below.

$$(a - b) \times (c - d) = a \times (c - d) - b \times (c - d) = (a \times c - a \times d) - (b \times c - b \times d) \\ = ac - ad - bc + bd$$

Let,

$$a = x^2, b = a^2, c = x, d = a$$

Now,

$$= x^2 \times (x - a) - a^2 \times (x - a) \\ = [(x^2 \times x) + (x^2 \times -a)] - [(a^2 \times x) + (a^2 \times -a)] \\ = [x^3 - x^2a - a^2x + a^3]$$

13. $(3p^2 + q^2)(2p^2 - 3q^2)$

Solution:-

Suppose $(a + b)$ and $(c - d)$ are two binomials. By using the distributive law of multiplication over addition twice, we may find their product as given below.

$$(a + b) \times (c - d) = a \times (c - d) + b \times (c - d) = (a \times c - a \times d) + (b \times c - b \times d) \\ = ac - ad + bc - bd$$

Let,

$$a = 3p^2, b = q^2, c = 2p^2, d = 3q^2$$

Now,

$$= 3p^2 \times (2p^2 - 3q^2) + q^2 \times (2p^2 - 3q^2) \\ = [(3p^2 \times 2p^2) + (3p^2 \times -3q^2)] + [(q^2 \times 2p^2) + (q^2 \times -3q^2)] \\ = [6p^4 - 9p^2q^2 + 2q^2p^2 - 3q^4] \\ = [6p^4 - 7p^2q^2 - 3q^4]$$

14. $(2x^2 - 5y^2)(x^2 + 3y^2)$ **Solution:-**

Suppose $(a - b)$ and $(c + d)$ are two binomials. By using the distributive law of multiplication over addition twice, we may find their product as given below.

$$(a - b) \times (c + d) = a \times (c + d) - b \times (c + d) = (a \times c + a \times d) - (b \times c + b \times d) \\ = ac + ad - bc - bd$$

Let,

$$a = 2x^2, b = 5y^2, c = x^2, d = 3y^2$$

Now,

$$= 2x^2 \times (x^2 + 3y^2) - 5y^2 \times (x^2 + 3y^2) \\ = [(2x^2 \times x^2) + (2x^2 \times 3y^2)] - [(5y^2 \times x^2) + (5y^2 \times 3y^2)] \\ = [2x^4 + 6x^2y^2 - 5y^2x^2 - 15y^4] \\ = [2x^4 + x^2y^2 - 15y^4]$$

15. $(x^3 - y^3)(x^2 + y^2)$ **Solution:-**

Suppose $(a - b)$ and $(c + d)$ are two binomials. By using the distributive law of multiplication over addition twice, we may find their product as given below.

$$(a - b) \times (c + d) = a \times (c + d) - b \times (c + d) = (a \times c + a \times d) - (b \times c + b \times d) \\ = ac + ad - bc - bd$$

Let,

$$a = x^3, b = y^3, c = x^2, d = y^2$$

Now,

$$= x^3 \times (x^2 + y^2) - y^3 \times (x^2 + y^2) \\ = [(x^3 \times x^2) + (x^3 \times y^2)] - [(y^3 \times x^2) + (y^3 \times y^2)] \\ = [x^5 + x^3y^2 - y^3x^2 - y^5]$$